

Publication 2 (2015)

Accuracies and Contrasts of Models of the Diffusion-Weighted-Dependent Attenuation of the MRI Signal at Intermediate b -values

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ABSTRACT: The diffusion-weighted-dependent attenuation of the MRI signal $E(\theta)$ is extremely sensitive to microstructural features. The aim of this study was to determine which mathematical model of the $E(\theta)$ signal most accurately describes it in the brain. The models compared were the monoexponential model, the stretched exponential model, the truncated cumulant expansion (TCE) model, the biexponential model, and the triexponential model. Acquisition was performed with nine b -values up to 2500 s/mm² in 12 healthy volunteers. The goodness-of-fit was studied with F -tests and with the Akaike information criterion. Tissue contrasts were differentiated with a multiple comparison corrected nonparametric analysis of variance. F -test showed that the TCE model was better than the biexponential model in gray and white matter. Corrected Akaike information criterion showed that the TCE model has the best accuracy and produced the most reliable contrasts in white matter among all models studied. In conclusion, the TCE model was found to be the best model to infer the microstructural properties of brain tissue.

KEYWORDS: diffusion MRI, model accuracy, kurtosis, cumulant expansion, Akaike information criterion, brain, IVIM

CITATION: Nicolas et al. *Accuracies and Contrasts of Models of the Diffusion-Weighted-Dependent Attenuation of the MRI Signal at Intermediate b -values*. *Magnetic Resonance Insights* 2015; 8: 1–21 doi:10.4137MRI.25235

RECEIVED: February 26, 2015. **RESUBMITTED:** April 23, 2015. **ACCEPTED FOR PUBLICATION:** April 26, 2015.

ACADEMIC EDITOR: Sandro Velan, Editor in Chief

TYPE: Original Research

FUNDING: This work was supported by the LECMA (Ligue Européenne Contre la Maladie d'Alzheimer), the EPHE (Ecole Pratique des Hautes Etudes), and by the 2013 joint fellowship of the CNFV (Société Française de NeuroVascular) and France AVC, dedicated to the study of the brain tissue microstructure. The funders had no influence over the study design, content of the article, or selection of the journal.

COMPETING INTERESTS: Authors disclose no potential conflict of interest.

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Introduction

Diffusion MRI (dMRI) is a powerful *in vivo* method for exploring biological microstructures.¹ The contrast of diffusion-weighted (DW) images is dependent on the magnitude of the diffusion-weighting factor (b -value). In clinical practice, especially for fast and early detection of ischemic stroke, DW images are generally acquired with a unique b -value ($b = 1000$ s/mm²). The geometric mean of DW images over three spatial directions is then used to calculate apparent diffusion coefficient (ADC) maps² with the help of a monoexponential model (MEM) formalism. As it uses the same limited range of b -values but is acquired for 6–60 spatial directions,³ diffusion tensor imaging is also an MEM that includes the effect of water diffusion anisotropy³ and leads to the calculation of a rotationally invariant form of the ADC , the mean diffusivity.

On the other hand, the higher the b -value, the more sensitive the DW images are to smaller absolute random displacements of water molecules, and therefore to the microscopic structures of brain tissue.¹ Therefore, high b -value dMRI consists of recording series of DW images with successively increasing b -values up to relatively high values (b –2500 to \sim 12,000 s/mm²). The number of spatial directions measures acquired is adapted depending on the time constraints. The

DW-dependent attenuation of the MRI signal obtained in each image pixel is related by Fourier transformation to the water displacement probability distribution (q -space method). In brain tissue, the standard deviation of this distribution has a characteristic length scale of tenths of μm ,^{4,5} making it possible to investigate some microstructural changes related to cerebral insults.⁵ However, Fourier transformation of the DW-dependent attenuation of the MRI signal (q -space) requires experimentally challenging conditions, whereas signal modeling is more flexible. Indeed, the DW-dependent attenuation of the MRI signal (designed as $E(\theta)$) acquired with intermediate or high b -values needs to be modeled numerically with a mathematical function describing its non-exponential decay, which is relevant to the postulated properties of the microscopic structures present in brain tissues.^{4,6–8} High b -value dMRI modeling and q -space are very sensitive to microscopic water displacements, highlighting white matter (WM) structures^{7,8} or cerebral insults in animals^{9–12} and in human brains,^{5,13} and thus having a potential clinical interest.

Two types of models are needed for the study of diffusion imaging. The first (signal models) describes empirically how the $E(\theta)$ signal decays, whereas the second (tissue models) describes how the signal relates to the underlying tissue

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